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WILDLAND FIRE PROBABILITIES ESTIMATED FROM
WEATHER MODEL-DEDUCED MONTHLY MEAN FIRE DANGER INDICES
*Haiganoush K. Preisler¹, Shyh-Chin Chen², Francis Fujioka², John W. Benoit² and
Anthony L. Westerling³*

¹ USDA Forest Service USDA, Pacific Southwest Research Station, 800 Buchanan St.,
West Annex, Albany, CA 94710 Telephone: +1 510 559-6484; fax: +1 510 559-6440;
corresponding author email: hpreisler@fs.fed.us

² USDA Forest Service USDA, Pacific Southwest Research Station, Riverside, CA.

³ University of California, Merced, CA

Running Head: Estimation of wildland fires probabilities

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1 *Abstract*

2 The National Fire Danger Rating System indices deduced from a regional simulation
3 weather model were used to estimate probabilities and numbers of large fire events on
4 monthly and one degree grid scales. The weather model simulations and forecasts are
5 ongoing experimental products from the Experimental Climate Prediction Center at the
6 Scripps Institution of Oceanography. The monthly average Fosberg Fire Weather Index,
7 deduced from the weather simulation, along with the monthly average Keetch-Byram
8 Drought Index and Energy Release Component, were found to be more strongly
9 associated with large fire events on a monthly scale than any of the other stand-alone fire
10 weather or danger indices. These selected indices were used in the spatially explicit
11 probability model to estimate the number of large fire events. Historic probabilities were
12 also estimated using spatially smoothed historic frequencies of large fire events. It was
13 shown that the probability model using four fire danger indices outperformed the historic
14 model, an indication that these indices have some skill. Geographical maps of the
15 estimated monthly wildland fire probabilities, developed using a combination of four
16 indices, were produced for each year and were found to give reasonable matches to actual
17 fire events. This method paves a feasible way to assess the skill of climate forecast
18 outputs, from a dynamical meteorological model, in forecasting the probability of
19 wildland fire severity with known precision.

1 **Introduction**

2 Since the US Forest Service (USFS) National Fire Danger Rating System (NFDRS) was
3 developed (Deeming *et al.* 1977), the indices of the system have been routinely
4 evaluated, updated and standardized at individual stations as a monitoring measure to
5 assess current fire danger at local and national scales. The NFDRS indices reflect
6 average worst case fire potential from the effects of terrain, weather and fuel conditions
7 represented by standard fuel models. Fuel moisture models use weather input such as
8 cumulative precipitation, temperature and relative humidity to determine moisture
9 content of the fuels. Federal, state and local wildland fire management agencies use the
10 NFDRS for quantification of risk, staffing levels, appropriate suppression response, and
11 strategic planning (NWCG Fire Weather Working Team 2005).

12 Clearly, the reliability and the integrity of the NFDRS depend partially on the
13 quality and quantity of input data obtained from weather stations. Typical difficulties
14 with fire weather station data include insufficient spatial coverage and inconsistent
15 maintenance of weather instruments. An alternative source of fire weather data for the
16 NFDRS is global or regional scale weather analysis in digital formats. A weather model
17 can provide not only dynamically consistent data with ample spatial coverage; it can also
18 provide weather predictions for dynamical forecasts of NFDRS indices with lead times
19 ranging from days to a season or longer.

20 Recently, Roads et al. (2005) evaluated experimental forecasts of NFDRS indices
21 at weekly to seasonal scales that used long-range weather predictions from a
22 meteorological model. They showed that these indices can be well predicted at weekly
23 time scales when compared with indices computed from weather model-generated one-

1 day forecasts, which they call validation data, because the one-day forecast data are used
2 to “validate” the weekly to seasonal forecasts . Some indices have prediction skill even at
3 seasonal scales, especially over summers in the western US. Similarly, Hoadley et al.
4 (2004, 2006) found that predicted surface weather variables from the fifth-generation
5 Mesoscale Model (MM5) and the daily corresponding NFDRS indices compared
6 reasonably well to the observed weather at selected stations and the corresponding
7 “observed” indices, calculated from the observed weather. Even if predicted fire indices
8 from weather models are skillful at various time scales, there is still a question as to how
9 these model-deduced indices correlate with actual fire statistics, such as number of large
10 fire occurrences and acres burned. Roads et al. (2005) found a rather weak relationship
11 between their monthly-mean validation indices and the observed fire counts or acres
12 burned. Part of their problem might have been the use of simple temporal correlation at
13 each grid point between the validation indices and the actual fire counts. Correlation
14 statistics are typically a poor measure of association when they involve count variables
15 that are small (most fire counts are zero or one). Alternative statistical analyses may
16 better describe associations between modeled fire indices and observed fire counts,
17 including counts of fires of different sizes. Moreover, strategic planning activities in a
18 seasonal time frame typically involve large areas, from regional to national scales, e.g.
19 the US fire season severity assessment. Further analysis is therefore warranted that
20 relates fire activity statistics from large areas to candidate fire weather and index
21 predictors. This paper focuses on the effectiveness of the model simulated NFDRS
22 indices in estimating large fire events.

1 Others have studied the skill of daily NFDRS indices, produced using weather
2 station data, in estimating probabilities of large fires. Simard et al. (1987) developed an
3 extreme fire potential index, based on NFDRS indices, and employed a threshold value of
4 the index that captured a large number of extreme fire event days with a minimum
5 number of false alarm days. Andrews and Bradshaw (1997) demonstrated how a logistic
6 model may be used to generate probability curves relating daily fire activity in a given
7 forest to NFDRS indices from the closest weather station. Preisler et al. (2004) developed
8 a spatially and temporally explicit logistic model, on a 1-km² –day scale, to estimate
9 probabilities of large federal fires in Oregon using NFDRS indices also from weather
10 stations.

11 In this study a probability model (Brillinger et al., 2003; Brillinger et al. 2006;
12 Preisler et al., 2004; Preisler and Westerling 2007) is used to evaluate the utility of the
13 weather model-simulated monthly fire danger variables, when used one at a time or in
14 combination, in estimating large fire events for the corresponding month. The estimated
15 probabilities are spatially explicit on a one-degree grid-cell level and temporally explicit
16 at a monthly scale. In the following sections we will first briefly introduce the weather
17 model and the NFDRS indices it generates, followed by a description of the observed
18 gridded monthly fire occurrence and acres burned data. The probability models and
19 statistical approaches will then be discussed before the result of the fire probability is
20 evaluated.

21 **Methods**

22 *Modeled Fire Weather and Danger Variables*

23 *Weather Model*

1 The fire danger variables in this study were adapted from Roads *et al.* (2005), in which
2 the meteorological forecasting system developed at the Experimental Climate Prediction
3 Center (ECPC) (Roads *et al.* 2003) was used. Specifically, the model system uses
4 operational daily 00 UTC analyses from the National Centers for Environmental
5 Prediction (NCEP) Global Data Assimilation (GDAS), which is used for the global
6 extended range weather forecast at NCEP, as initial condition for a regional forecast with
7 up to 16 weeks lead time. The original higher resolution global analysis was first linearly
8 transformed to a triangular truncation of T62 (192×94 global Gaussian grid, roughly 150
9 km grid space resolution at 40°N) and 18 vertical levels so that the subsequent seasonal
10 scale regional forecasts could be done with the available computer resources.

11 The regional spectral model (RSM) used in this study was originally developed at
12 NCEP (Juang and Kanamitsu 1994; see also Juang *et al.* 1997). The RSM is a regional
13 extension of the global spectral model (GSM; Kalnay et al 1996). In particular, the RSM
14 provides an almost seamless transition from the GSM to the higher resolution region of
15 interest (Chen *et al.* 1999) and thus avoids a common regional model problem when
16 using incompatible physics between the driving global model and the nested regional
17 model (Chen 2001). Except for the scale-dependence built into the horizontal diffusion
18 and some minor adjustment to other physical parameterizations, the GSM and RSM
19 physical parameterizations are, in principle, identical. A modeling system such as the
20 GSM to RSM used here is particularly helpful in isolating the regional downscaling
21 problems caused by potential mismatched model physics between the regional and
22 driving global model (Chen 2001). More discussion of the updated model physics can be

1 found in Hong and Pan (1996). The description of the RSM and the model setup used in
2 this study can be found in Roads et al. (2003).

3 *Modeled NFDRS Indices*

4 Global analysis from January 1, 1998 through December 31, 2003 was used to initialize
5 the GSM. The 4 times daily output of the one-day forecasts of GSM were then used as
6 initial and lateral boundary conditions of the RSM for one day integration for each initial
7 day. Horizontal grid spacing of 60 km was used in the RSM. The one-day forecasted
8 surface weather variables, including temperature, two-meter relative humidity (R2H) ,
9 wind speed from the model, and top 10-cm soil moisture content (SMC1) along with
10 observed precipitation, fuels and slope, were the input for the NFDRS indices
11 computation (Burgan 1988). The major differences of our NFDRS calculation from the
12 standard one is the use of weather model 1-day forecast output, instead of weather station
13 observations. However, in order to avoid the precipitation spin-up problem caused by the
14 imperfect initial condition of the meteorological model for short period integration, the
15 $0.25^\circ \times 0.25^\circ$ observed precipitation (Higgins *et al.* 2000), instead of model precipitation
16 output, was used in computation. Monthly indices used in this study were subsequently
17 derived from the daily indices. Interested readers should refer to Roads *et al.* (2005) and
18 Burgan (1988) for a more detailed description of the NFDRS indices computation. Since
19 not all standard NFDRS indices are useful to fire managers, we chose to examine only
20 spread component (SC), energy release component (ER), burning index (BI), ignition
21 component (IC) and Keetch-Byram (KB) drought component. In addition, Fosberg fire
22 weather index (FFWI, see description below), R2H, and SMC1 from the meteorological
23 model were also included to contrast the skill from NFDRS indices.

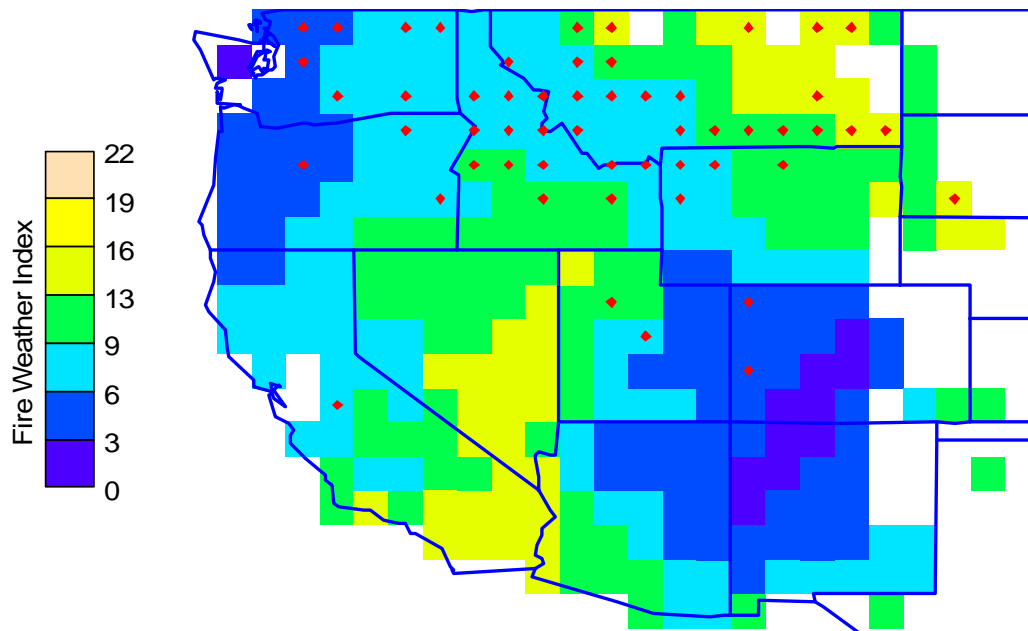
1 FFWI (Fosberg 1978; Fujioka and Tsou 1985), an index derived only from
2 temperature, relative humidity and wind speed, assumes constant grass fuel and
3 equilibrium moisture content as a function of the input weather variables. This index is
4 not part of the NFDRS and requires only instantaneous values from a weather model.
5 Due to its ease of application, FFWI has been used for seasonal fire danger forecasting to
6 provide a first look of global wildfire condition (Roads *et al.* 1995). As will be shown,
7 despite its use of constant fuel information, FFWI offers a significant skill in explaining
8 the fire occurrence at a monthly scale.

9 All model deduced indices from 1-day GSM/RSM forecasts were called
10 ‘validating’ indices in Roads *et al.* (2005). In the present work these monthly mean
11 indices are used as surrogates for ‘observed’ values, since one-day forecasts have been
12 found to be very skillful when compared to observations. Interested readers should refer
13 to Roads *et al.* (2005) for detailed descriptions.

14 ***Fire Occurrence Data***

15 This work relied on fire history data sets over the western US compiled from federal land
16 management agency fire reports. Westerling *et al.* (2003) compiled a gridded one-degree
17 latitude/longitude (317 grid cells) data set of monthly fire starts and acres burned from
18 approximately 300,000 fires reported by the USDA Forest Service, the USDI’s Bureaus
19 of Land Management and Indian Affairs, and the National Park Service for 1980-2004.
20 However, since we have meteorological model-derived fire danger indices from January
21 1998 through December 2004, we only used the fire data for the same period. A map of
22 the monthly-mean fire weather index (FFWI) and the locations of large fire events (area
23 burned > 400 ha \approx 1000 acres) for August 2003 (Figure 1) shows the geographic region

1 and the structure of the spatially and temporally explicit explanatory variables used in
2 this study.



3
4 **Figure 1:** Map of study area (Western US) showing the one-degree grid cells and values of the
5 Fosberg Fire Weather Index for August 2003. Red dots indicate locations of large fire events
6 (area burned > 400 ha \approx 1000 acres) reported on federal lands for the month of August 2003.
7

8 *Statistical Methods*

9 *Probability models*

10 The statistical approach is based on developing a semi-parametric logistic regression
11 model (Hastie et al. 2001, Preisler and Westerling 2007) using historic monthly fire
12 occurrence data as the dependent variable and weather modeled NFDRS indices as the
13 independent variables.

1 The regression model estimates two fire danger probabilities: probability of fire
2 occurrence and conditional probability of large fire event. Probability of fire occurrence
3 was defined as the probability of at least one fire of any size occurring in a given one-
4 degree grid cell during a given month of a year. The probability of a large fire event was
5 defined as the probability of the occurrence of a burn area greater than 400 ha (\approx 1000
6 acres) given at least one fire occurrence in the one-degree cell during a given month of a
7 year. The product of the above two probabilities was used as a measure for fire danger.
8 The 400 ha cut-off for large fires, although arbitrary, aligns with size class F fires. The
9 same methods may be used to estimate probabilities of area burned of any particular size.

10 The explanatory variables used in the regression model were the modeled NFDRS
11 indices described above in addition to a purely temporal variable (month-in-year) and a
12 geo-spatial vector variable (latitude and longitude of the one-degree grid cell). The
13 temporal variable (month) was included in the model as a proxy for annual cyclical
14 patterns of fire occurrence and large fire events that may not have been properly captured
15 by the indices. The geo-spatial vector (latitude, longitude) was included in the regression
16 as a surrogate for variables with spatial patterns (e.g. vegetation type, elevation or human
17 activities) that do not change over time. Smooth nonparametric functions of the
18 explanatory variables were used instead of parametric functions, e.g. polynomials,
19 because it is anticipated that relationships between the explanatory variables - in
20 particular between latitude, longitude, month – and large fire occurrence may be complex.
21 Consequently, these relationships will be better characterized by flexible nonparametric
22 functions such as piece-wise polynomials and splines. Further details of the estimation
23 procedure, including the estimation of the smooth functions, can be found in the

1 Appendix. See also Brillinger et al. (2003), Preisler et al. (2004), and Preisler and
2 Westerling (2007).

3 Although our estimates were based on a large number of observations (monthly
4 values on 317 grid cells and six years for a total of 22,824 voxels), these observations are
5 likely to be correlated, in particular if there is a strong yearly effect (e.g, overall dry years
6 etc.). Consequently, all standard errors were calculated using the Jackknife procedure
7 (Efron and Tibshirani 1993). Jackknife standard errors were produced by developing six
8 different estimates of the model parameters (each time using data from all years but one),
9 then calculating the Jackknife standard error of the resulting estimates.

10

11 *Mutual Information Statistics*

12 We used the Mutual Information (*MI*) statistic (Brillinger et al. 2004) to study the
13 strength of the statistical dependencies between explanatory variables (e.g. indices) and
14 the probabilities of fire danger. In particular, we used the *MI* statistic to select the index,
15 or combination of indices, with the most ‘information’ regarding the probability of fire
16 danger. The *MI* statistic is similar to the Akaike Information Criteria (*AIC*), and it is
17 equivalent to the variance explained if both involved variables are Gaussian distributed.
18 Further details regarding the *MI* statistic are given in the Appendix. The following
19 models were compared using the *MI* statistic:

20 1) Historic (climatologic) model (H)

21 The only explanatory variables used in this model were month-in-year and
22 location (latitude, longitude). With this model each cell has a different probability
23 for each location and month of the year but the probabilities do not change from

1 year to year. The historic model is a spatially and temporally smoothed version of
2 the relative frequencies of observed large fire events for each month of the year
3 and each pixel.

4 2) Fire danger index model (X)

5 The explanatory variables in this model include spatial location, month and one
6 fire danger index. Consequently, probabilities in each cell change with location,
7 month in year, and the value of the fire danger index. One model was produced
8 for each index and named after the index.

9 3) Multiple indices model (C)

10 The explanatory variables in this model were spatial location, month and a
11 combination of two or more fire danger indices.

12 The multiple indices model with the ‘best’ selection of indices was next used to
13 estimate the probabilities of fire occurrence and the conditional probability of a large fire
14 event. Finally the unconditional probability of a large fire event, i.e., the probability that
15 an area of size greater than 400 ha will burn in a one-degree grid cell in a given month
16 and year, was estimated by multiplying the above two estimated probabilities.

17

18 *Assessing Model Skill*

19 We assessed the goodness-of-fit of the final selected model by producing reliability
20 diagrams (Hosmer and Lemeshow 1989, Wilks 1995). The latter was done by grouping
21 together all cells with similar estimated probabilities (within 3% of each other) and
22 comparing the observed fraction of responses in each group with the corresponding
23 estimated probability of response. A response here was defined as a voxel (one-degree x

1 one-degree x month) with a large fire event. Estimated probabilities for each voxel were
2 produced using cross-validation. Specifically, estimations for a given year were done by
3 using the model parameters from all other years except the year being evaluated.

4 In an alternative assessment of goodness-of-fit we studied the skill of the model in
5 estimating the distribution of total number of grid cells per month with large fire events
6 by comparing observed numbers of monthly totals for each year with the estimated 50th
7 and 95th percentiles. The estimated percentiles included both natural variation (Poisson)
8 and variation due to the error in the estimated model parameters.

9

10 *Fire Danger Maps*

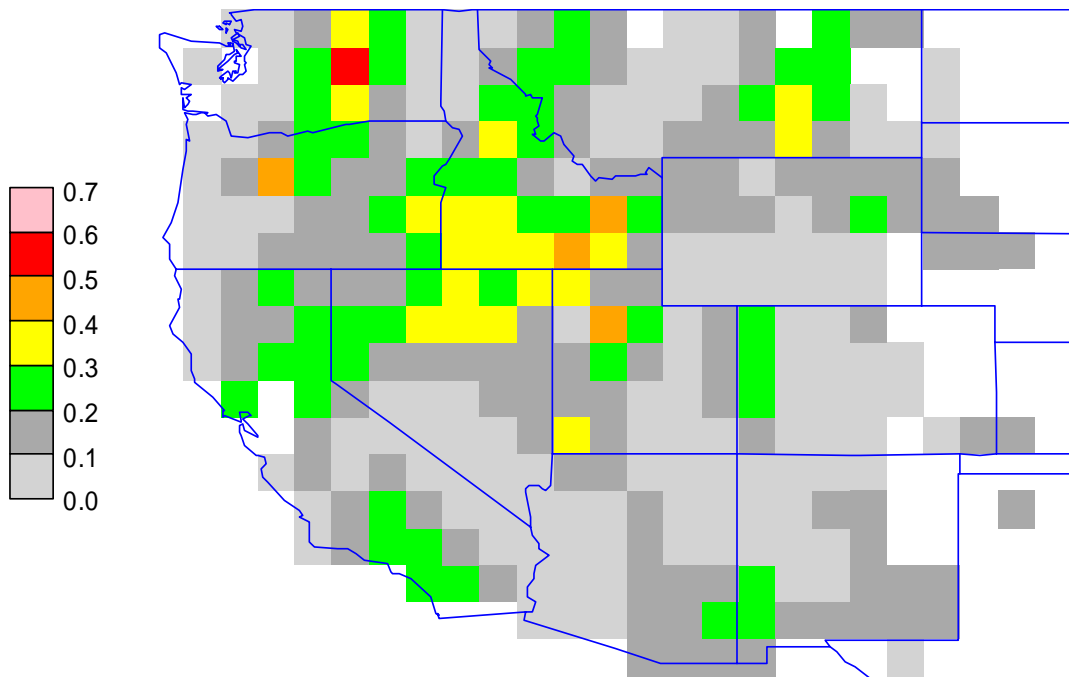
11 We produced two types of fire danger maps. The first was based on estimated
12 probabilities of large events using the following rule: Let \hat{p} be the estimated probability
13 of area burned > 400 ha and SE be an estimate of the standard error of \hat{p} . Then fire
14 danger was defined as

15	Low	if	$\hat{p} + 2SE \leq 10\%$.
16	Moderate	if	$10\% < \hat{p} + 2SE \leq 30\%$.
17	High	if	$30\% < \hat{p} + 2SE \leq 50\%$.
18	Extreme	if	$\hat{p} + 2SE > 50\%$.

19 The size of areas burned (400 ha) and the cutoff probabilities used above are for
20 demonstration purposes only. Managers may decide on other cutoff points for what may
21 be considered a large fire event or acceptable levels of risk. Note that, although
22 conditions are defined as extreme when the probability of a large fire event is > 50% the
23 frequency of times a voxel is designated as extreme is very small. During the six years of

1 our study ‘extreme’ conditions were observed in only 120 voxels (0.5% of cases), of
2 those cases 63 (52.5%) were actually large fire events.

3 The second set of danger maps was produced to demonstrate departures from
4 ‘normal’ conditions, or anomalies. In this study the ‘norm’ was the estimated probability
5 of a large fire event produced by using the H model. Since our study was based on six
6 years of data (1998-2003) the ‘norm’ reflected average conditions during these six years.
7 For example, Figure 2 shows the July historical probabilities of large fire events. Highest
8 historic probabilities during the six years of study appear to be in the Washington,
9 southern Idaho and Northern Nevada regions.



10

11 **Figure 2:** Probabilities of large fire events for the month of July estimated from historic fire
12 occurrence and size data for the period of 1998-2003.

1

2 Maps of estimated departure from the norm were produced using the odds ratio
3 statistic. Specifically, maps were produced of the odds of a large event relative to the
4 historic odds as estimated by the given six years of observed fire data. The rules used to
5 produce the maps were as follows: define $\hat{\pi}_C$ and $\hat{\pi}_H$ as the probabilities of an area
6 greater than 400 ha burning in a given voxel estimated using the C and the H models,
7 respectively. Let $\hat{\theta} = \log(\hat{\gamma})$ be the logarithm of the estimated odds
8 ratio, $\hat{\gamma} = \hat{\pi}_C / (1 - \hat{\pi}_C) \div \hat{\pi}_H / (1 - \hat{\pi}_H)$, i.e. the logarithm of the odds relative to historic
9 values. Fire danger maps were produced using the rules:

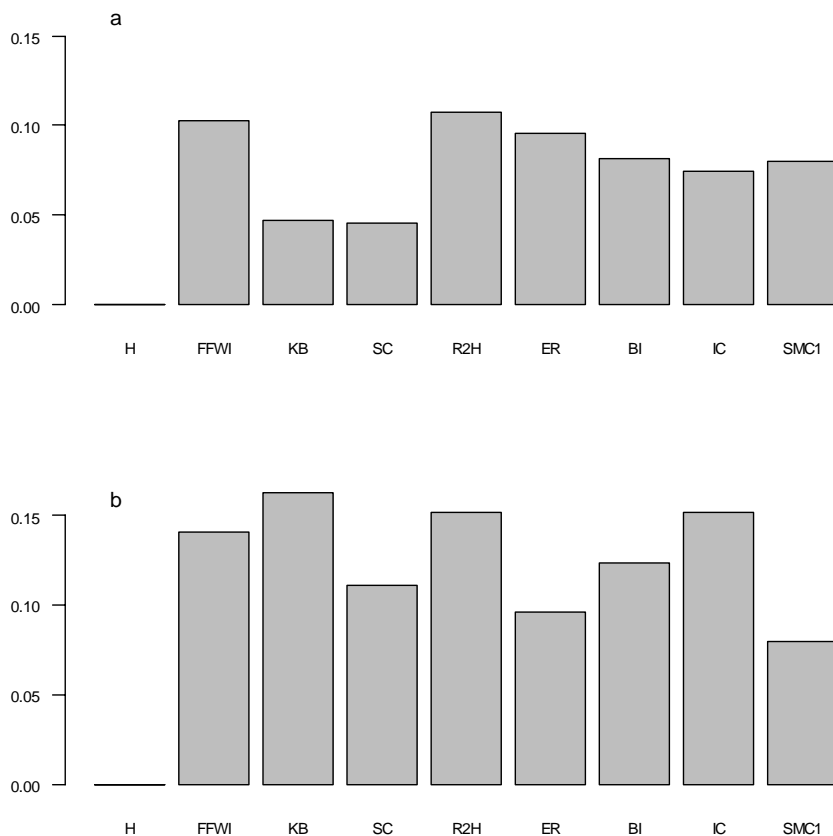
	Lower than historic	if $\hat{\theta} + \hat{\sigma} < 0$	
10	Normal	if $-\hat{\sigma} \leq \hat{\theta} \leq \hat{\sigma}$	[1]
	Higher than historic	if $\hat{\theta} - \hat{\sigma} > 0$	

11 With the above rule a voxel is designated as normal if the log-odds of a large fire event
12 for a given month are within one standard deviation ($\hat{\sigma}$) from the historic odds for that
13 month (i.e., odds ratio equal one, or equivalently logarithm of odds equal zero). A voxel
14 is designated as higher than historic if the log-odds for a large fire event are greater than
15 one standard deviation from the historic odds.

16 **Results**

17 Plots of standardized mutual information statistics for various models (Figure 3)
18 demonstrate the relative importance of each fire danger or fire weather index on the
19 probability of fire occurrence and conditional probability of large fire event. All MI
20 values in the plot are relative to the H model. The standardized MI for the H model was
21 set to zero. The two indices, FFWI and R2H indicated the highest relative increase in

1 strength of dependence with fire occurrence (Figure 3a) when added individually to the H
 2 model. The linear correlation between R2H and FFWI is high ($r = -0.92$). The latter is
 3 expected because R2H is one of the input variables for computing FFWI. Indices with
 4 highest relative increase in strength of dependence with the conditional probability of a
 5 large fire event were KBDI, FFWI, IC and R2H (Figure 3b).

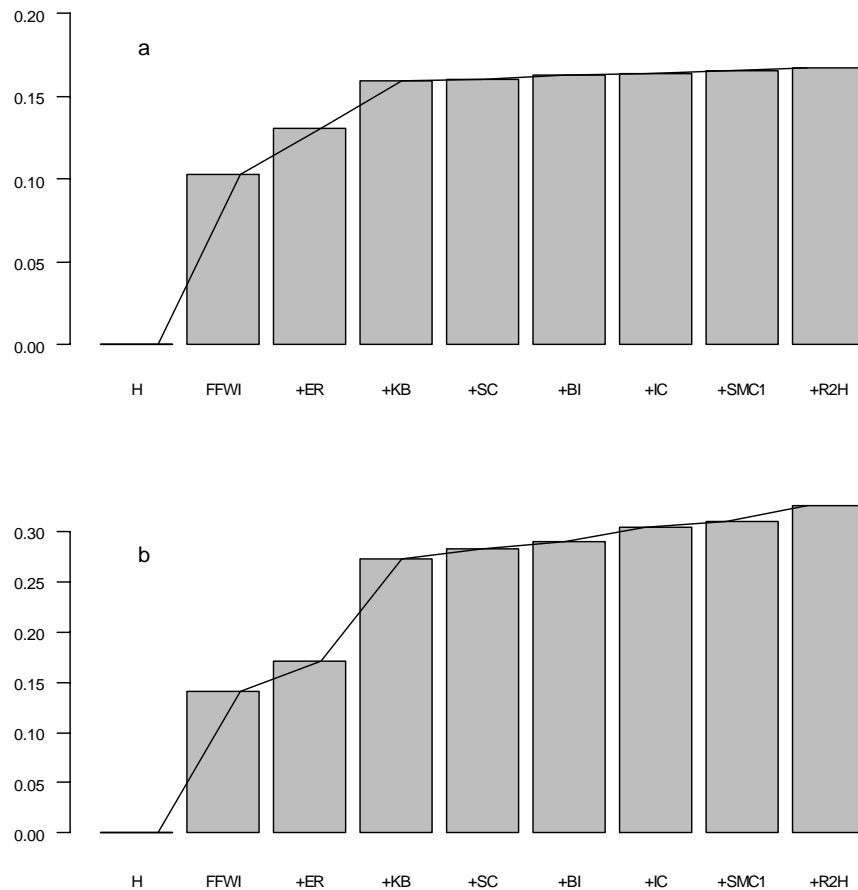


6

7 **Figure 3:** Standardized mutual information statistic describing the dependence of (a) probability
 8 of fire occurrence and (b) conditional probability of a large fire event on each fire danger/weather
 9 index when added to the historic model. All values are relative to the historic (H) model value
 10 which was set to zero. The height of each bar is the fraction increase in MI when an index (e.g.
 11 ER) is added to the historic model, i.e. $(MI_{ER} - MI_H)/MI_H$.
 12

13 Models with multiple indices were developed by adding indices one at a time to
 14 the historic model starting with FFWI. Values of the MI statistic estimated for each of the

1 models are presented in Figure 4. We chose to start with FFWI because it was the index
 2 that showed dependence with both probabilities of fire occurrence and conditional
 3 probability of large area burn. The order in which the indices were added to the
 4 probability model was such that those with the smallest correlation with FFWI were
 5 added first. For example, the column labeled +KB is the standardized MI produced for a
 6 model with the combination of the indices FFWI, ER and KB in addition to the variables,
 7 location and month, that are in the historic model.



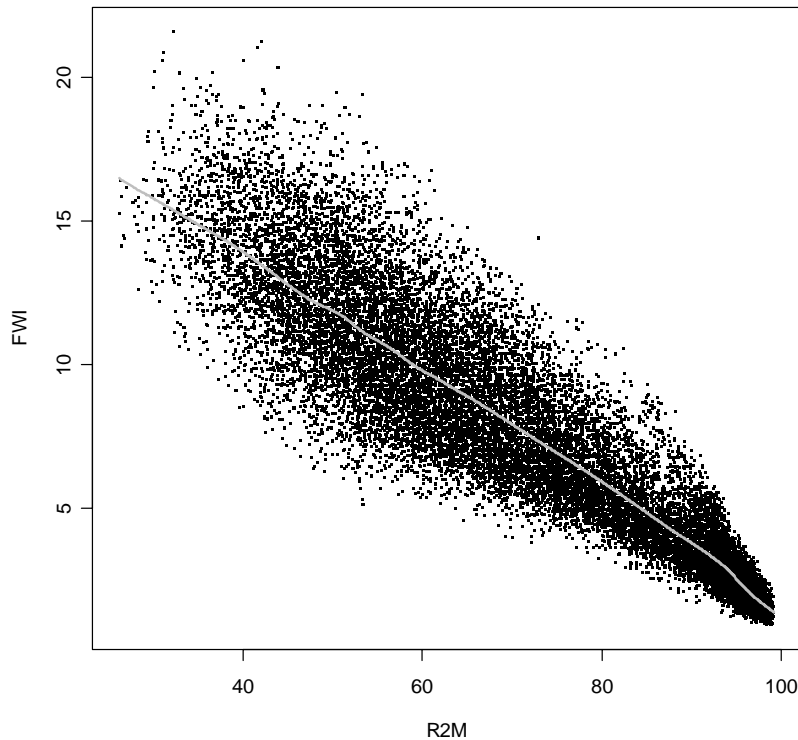
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9 **Figure 4:** Standardized mutual information statistic for models with multiple indices. All values
 10 are relative to the historic (H) value which is set to zero. The models were developed by adding
 11 indices consecutively in the order seen in the figures (left to right).
 12

1 Standardized values of MI increased with each addition of a new index to the H
2 model (Figure 4). However, increases after the first few indices were relatively small.
3 The final model (C) for the probability of fire occurrence used in the rest of the paper
4 included the indices FFWI, ER and KBDI. The final model for the conditional probability
5 of large fire included FFWI, ER, KBDI and R2H. The multiple indices model may be
6 thought of as a probability model based on a ‘new’ index which consists of a combination
7 of the four indices, FFWI, ER, KBDI and R2H.

8 Interpreting effects of explanatory variables is not easy particularly when the
9 variables are correlated. For example, R2H is inversely proportional to FFWI ($r = - 0.92$,
10 Figure 5). However this relationship appears to be less well defined during dry (low R2H)
11 and high FFWI weather. The variability around the mean increases with increasing FFWI
12 and decreasing R2M, and the correlation decreases (when $R2M < 50$ and $FFWI > 10$, $r =$
13 $- 0.37$). Consequently, it is not surprising that both R2M and FFWI contribute significant
14 information to the model. Wind may be playing a critical role under the circumstances.

15 Since the purpose of our statistical model is to estimate probability of fire danger,
16 the ultimate test of a given model with a selected set of indices is its skill in describing
17 observed events. To demonstrate the skill of estimating the occurrence of large fire
18 events, we plotted the observed fraction of large fire events *vs.* the estimated probabilities
19 from the H and the C models (Figure 6). The observed fraction is the number of cases
20 with observed large fire events as a percentage of the number of cases at each estimated
21 probability level. The scatter points of observed fractions of large fire events



1

2 **Figure 5:** Scatter plot of FFWI values against R2M. The variability around the mean level is seen
 3 to increase under dry conditions - higher values of FFWI and lower values of R2M.

4

5 were mostly within the expected point-wise 95% confidence bounds, which are

6 represented by the two dashed lines, for both models. The larger confidence bounds for

7 larger probabilities are likely due to the small number of cases at the higher probability

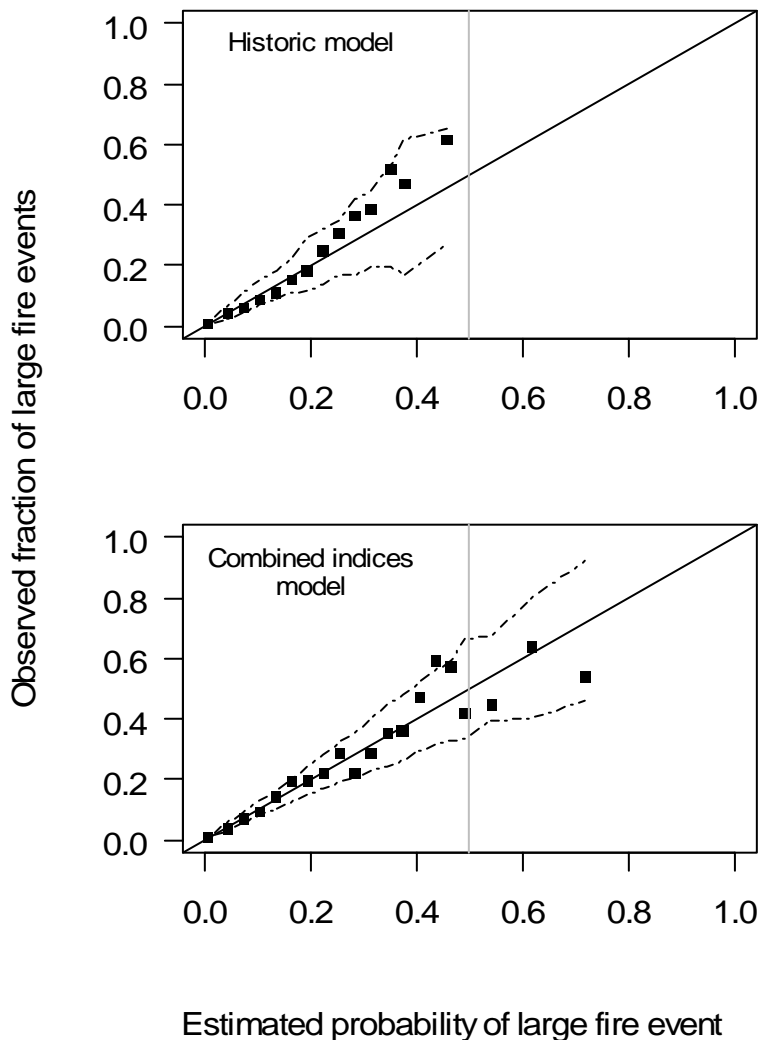
8 groupings. The overall Chi-square goodness of fit statistic improved from 36.8 (P-value =

9 0.0008) for model H to 19.2 (P-value = 0.51) for model C. Moreover, estimated

10 probabilities using model C spanned a wider range of values (0 to 0.72) than those of the

11 historic model H estimates (0 to 0.56). A model with no skill will have the same estimate

12 (no range in the values) for all locations and times.

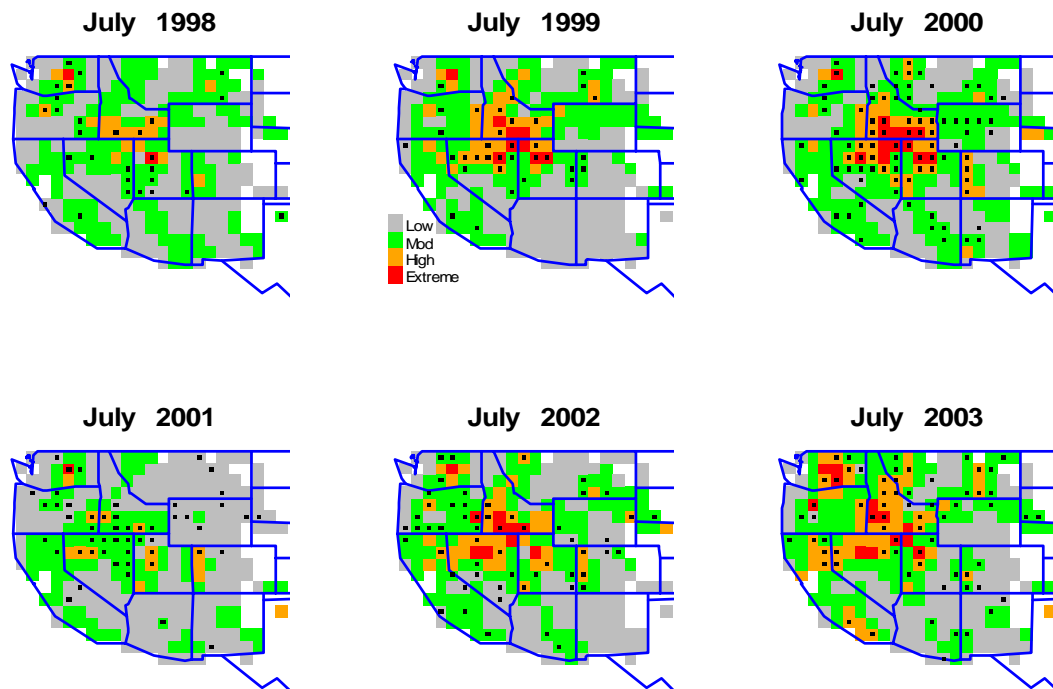


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2 **Figure 6:** Reliability diagrams showing the observed fraction of large events plotted against
 3 estimated probability for: (top) the historic model and (bottom) multiple indices model. Dashed
 4 lines are the approximate point-wise 95% confidence bounds.
 5

6 Fire danger maps, based on the final multiple indices model, were produced for
 7 each July from 1998 through 2003 (Figure 7) along with the location of events that
 8 actually occurred. In these maps a cell was designated as low danger if the estimated
 9 probability of an event was significantly less than 10%; moderate if the estimated
 10 probability was between 10%-30%; high if the estimated probability was between 30%-

1 50%; and extreme if the estimated probability was significantly greater than 50%. The
2 skill of the model for estimating large fire events at a given grid cell seems reasonable
3 when observed response (presence/absence of a large fire event) at a given grid and
4 month was compared with estimated fire danger. The maps presented here (Figure 7) and
5 similar maps for other months (not shown) may be used by fire managers to assess the
6 spatial and temporal fire danger. However, with intense fire potential during every fire
7 season over the West, these maps do not highlight anomalies.



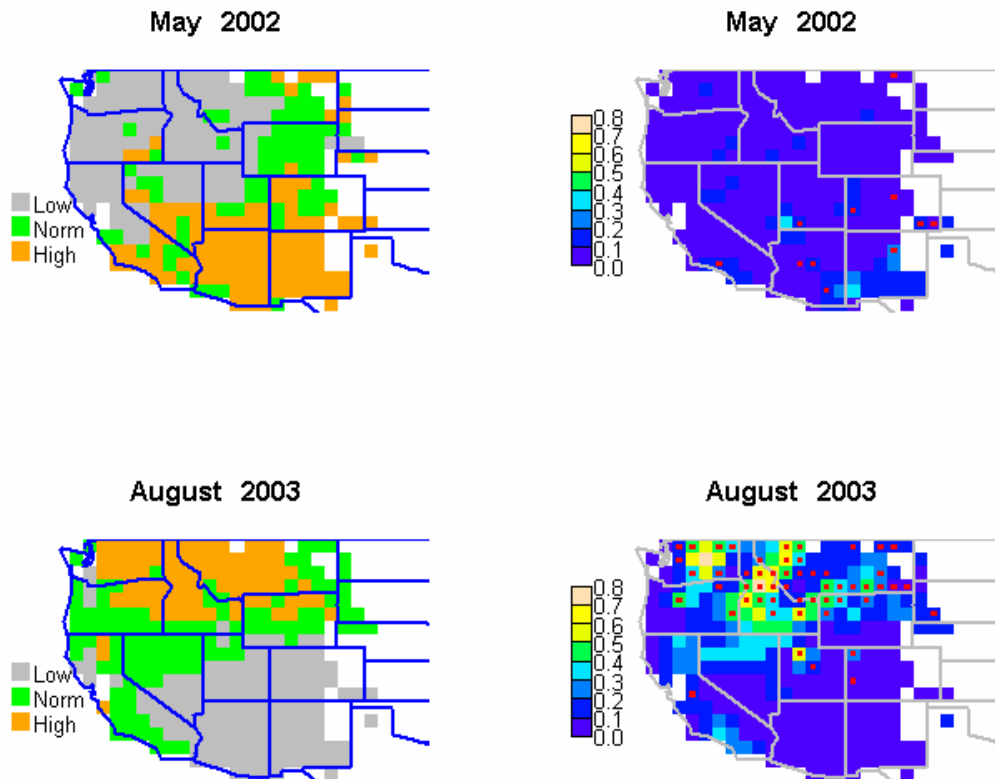
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9 **Figure 7:** Observed cells with large fire events (dots) and maps of fire danger based on estimated
10 probabilities of large fire events.

11

12 An alternative set of maps showing anomalies are those based on departure from
13 normal conditions, as given by estimated odds ratios relative to historic estimates (see Eq.
14 1). Maps of odds ratios are particularly useful when accompanied by maps of estimated

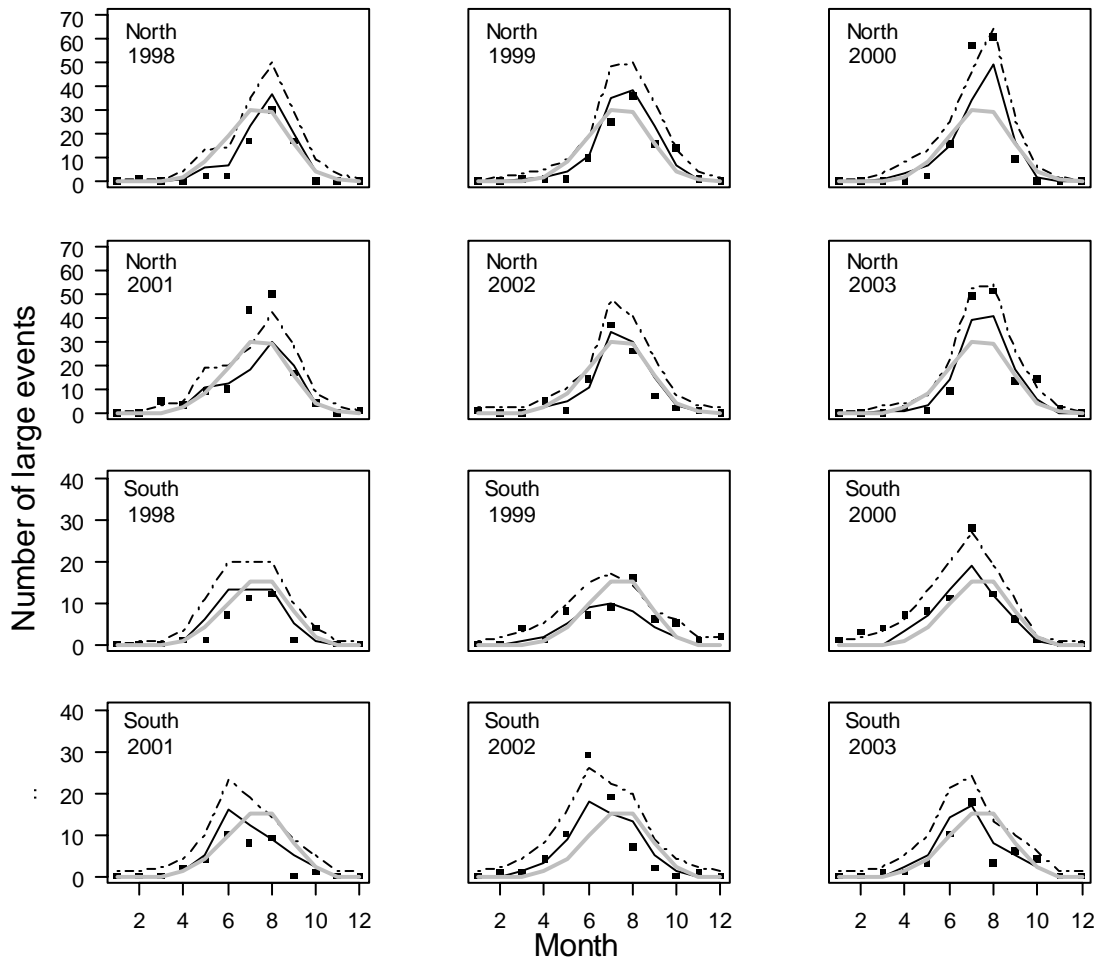
1 probabilities of large fire events. For example, the estimated odds of a large fire event
2 appeared to be higher than the norm in the southwestern states during May 2002 and in
3 the northwestern states in August 2003 (Figure 8 left panels). The estimated probabilities
4 for May 2002 in the Southwest (Figure 8 top right panel), although higher than normal,
5 were nevertheless quite low (<20%). The small number of observed events is consistent
6 with the low probabilities. On the other hand, in August 2003 the estimated odds for the
7 northwestern states were higher than the norm and the probabilities were also high
8 (mostly > 50%). Many large fire events were observed during this period.



9

10 **Figure 8:** Maps of odds relative to historic (left panels) and estimated probabilities (right panels)
11 of large fire events for two time periods. Red dots indicate locations of observed events during
12 that period.
13

1 Another useful output of the probability model is the estimated total number of
2 large fire events. Totals were obtained by adding the estimated probabilities over all cells
3 in a region. For example in Figure 9 we show the monthly estimated, as well as the
4 observed, large fire events for the northwestern and southwestern states separated at 40°N
5 latitude. The plots give the estimated 50th and 95th percentiles (solid curves) and the
6 observed numbers of cells with large fire events (dots). The 50th percentiles estimates
7 from the historic model are also given in grey lines. Historically, the Southwest appeared
8 to lag the Northwest by one month in reaching the peak of large fire occurrence during
9 the fire season. Over the northwestern region, higher than normal numbers of big fire
10 events were observed, and well estimated, for years 2000 and 2003. In summer 2001 the
11 observed number of cells with large fire events was greater than the upper 95th percentile.
12 Using estimated 95th percentiles one expects observations to exceed this level
13 approximately 5 percent of the time. In the southwestern region, the inter-annual
14 variations of fire events were not as apparent during the 6 years of our study. However,
15 summer of 2002 shows an observed early peak in June, compared to the historical model.
16 The latter was well captured in the estimates produced by the multiple indices model. The
17 higher and lower odds relative to historic estimates over the northwestern and
18 southwestern states for May 2002 and August 2003 respectively (Figure 8), can also be
19 found in the figures of monthly totals (Figure 9). Overall, the observed numbers were
20 distributed around the 50 percentile estimates with 4.1% (6/144) of the cases above the
21 95th percentile curve. In our example we used arbitrary north and south regions. Similar
22 estimates may also be produced for smaller areas such as individual Geographic Area
23 Coordination Centers (GACCs) for fire management use. Even though our results were



1

2 **Figure 9:** Observed (dots) and estimated (curves) number of one-degree cells with large fire
 3 events. Solid curves are the estimated 50th percentile of the fitted distribution. Dashed curves are
 4 the estimated 95th percentile of the distribution. Grey curves are estimated 50th percentiles of
 5 historic model.

6

7 based on a large number of observations, the time span of the study was only six years. It
 8 remains to be seen if the same selected variables will give similar skill when tested on
 9 other years with more, or less, severe fire seasons.

10

11 **Summary and Discussion**

12 A statistical method of estimating probabilities of large wildland fire events has been
 13 applied to the monthly mean fire danger indices produced by the numerical weather

1 prediction products from the ECPC. The derived indices with the most information for
2 estimating monthly probabilities of large fire events were FFWI, KBDI, ER, and R2H.
3 No additional information appeared to be gained by adding further indices to those listed
4 above. These variables were subsequently chosen to construct a combined index that was
5 used to estimate monthly probabilities of large fire events on a one-degree grid cell over
6 the western United States. The estimated probabilities were then compared with observed
7 frequencies of large events in order to assess the skill of the model.

8 Probability models, such as the one described here, are not only practical for
9 selecting variables and producing maps of fire danger, they are also useful in assessing
10 the skill of the fire danger indices in estimating (and eventually forecasting) frequencies
11 of wildland fire events. NFDRS was probably originally designed to support fire fighting
12 tactics on a daily basis. Some of the indices, such as SC, BI and IC, are sensitive to short
13 term variation of weather components, especially wind speed. These indices, therefore,
14 might lose their high frequency characteristics when a long term (e.g. monthly) average is
15 taken, as was the case in this study. Thus it is not surprising to see that some of these
16 model-derived indices did not contribute additional information to those slow varying
17 indices, such as KB and ER, in describing observed large fire events. What is surprising
18 is that FFWI, an index determined by weather variables alone, appeared to have a
19 significant contribution to the probability of large fires. Further analysis, possibly at the
20 daily time-scale, is required.

21 It is promising that a combination of fire danger indices appeared to have some
22 skill in estimating the probability of large fire events at a monthly scale. Adding a select
23 set of indices to the historic model appeared to improve the skill of the model in

1 estimating expected numbers of large events. Furthermore, estimated probabilities at each
2 cell may be developed into monthly anomaly maps for fire danger. The probability maps
3 showed reasonable agreement with the observed fire events.

4 While probability maps are useful in identifying high fire danger areas to fire
5 managers, a more useful application may be the ability to compare the total number of
6 large fire events against historic estimates over a region in a probabilistic manner. Roads
7 et al. (2005) showed that although the meteorological model predicted fire danger indices
8 reasonably well even at seasonal time scale, the associations (as measured by the
9 correlation coefficient) between the observed fire occurrence/acreage-burned and their
10 “observed” (validating) fire danger indices were poor. Part of the reason could be that
11 point-to-point temporal correlation is not adequate when describing nonlinear
12 relationships between variables that are not Gaussian. Additionally, correlation studies to
13 evaluate FDRS indices are not suitable for estimating or forecasting frequencies of fires.
14 Here we have proposed an alternative procedure for evaluating the association between
15 derived fire danger indices and fire characteristics that may also be used to estimate, and
16 eventually forecast, frequencies of large fires with known precision. The results indicated
17 that the estimated distribution of the number of large fire events agrees reasonably well
18 with those observed.

19 Similar analyses need to be done with forecasted fire weather/danger indices to
20 assess the skill of the forecasted variables on predicting large fire events in order for this
21 method to be truly useful for fire managers. Future work will address the skill of
22 predicting large fires at different lead times and at smaller temporal and spatial scales.
23 With fire occurrence data at the individual fire scale and forecasted fire weather/danger

1 indices at the daily and 1 km scale we should be able to develop forecasts over small
2 regions within administrative units so that the prediction can be used for fire management
3 operation.

4

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9 and Atmospheric Administration's Office of Global Programs via the California
10 Applications Program.

11

12 **Appendix**

13 The logistic regression lines used to estimate the probabilities of fire occurrence and large
14 fire events is specified in the following equation

$$15 \quad \text{logit}(p_v) = \beta_o + g_1(lon_v, lat_v) + g_2(month_v) + \sum_{m=1} h_m(X_{mv}) \quad [A1]$$

16 where the subscript, v , indicates the one-degree by one-month voxel; p is set to either the
17 probability of ignition or conditional probability of large fire given ignition; (lon, lat) are
18 the longitude and latitude of the midpoint of the grid cell; X_m are explanatory fire weather
19 and fire danger variables. The function h is a nonparametric smoothing function (Hastie
20 et al. 2001); g_2 is a periodic spline function (for estimating month-in-year effect); and g_1
21 is a thin plate spline function (for estimating the spatial surface as a function of lon and
22 lat). Estimation was done with the R statistical package (R Development Core Team,
23 2004). The procedure within the R package consists of first running the bs (basis spline)

1 function on each of the explanatory variables, then using the outputs from the bs runs as
 2 the new explanatory variables in a simple logistic regression routine. A periodic spline
 3 function (bs.per) is used for the month variable to allow for a smooth transition between
 4 the months of December and January. For the two-dimensional spline function of (*lon*,
 5 *lat*) the thin plate spline function (ts) is used to produced the necessary variables.

6 The *MI* statistic was defined as follows: let *Y* indicate the occurrence of a fire (or
 7 alternatively, a large fire event) and *X* indicate the logit line (linear predictor) as
 8 described in Eq. A1, then the *MI* statistic is given by

$$9 \quad MI_{X,Y} = E \left\{ \log \frac{p_{X,Y}(X,Y)}{p_X(X)p_Y(Y)} \right\} \quad [A2]$$

10 where $p_{X,Y}(X, Y)$, $p_X(X)$ and $p_Y(Y)$ are the joint and marginal distributions of *X*, *Y*
 11 respectively. For the bivariate normal case $1 - e^{-2MI_{X,Y}}$ is the coefficient of determination.
 12 In general, $MI_{X,Y} = 0$ when *X* and *Y* are independent and $MI_{X,Y} \leq MI_{Z,Y}$ if *Y* is independent
 13 of *X* given *Z* (Brillinger 2004). A similar and more commonly used statistic for choosing
 14 between models is the Akaike information criterion (*AIC*) given

15 by $AIC_{X,Y} = -2E \left\{ \log \frac{p_{X,Y}(X,Y)}{p_X(X)} \right\}$. Although *AIC* and *MI* often give similar results, as

16 was the case in the present study, *AIC* does not have the same interpretation as the *MI*
 17 statistic as a measure of the strength of statistical dependence.

18

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1 SUMMARY

2 Fire danger indices evaluated from a regional simulation weather model were used to
3 estimate probabilities of large fire events on monthly and one degree grid scales. This
4 paves a way to assess the skill of climate forecast outputs in predicting wildland fire
5 severity with known precision.

6